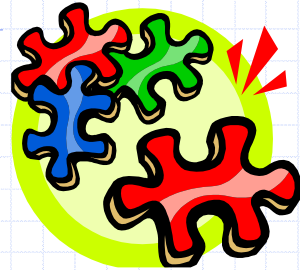


Sets



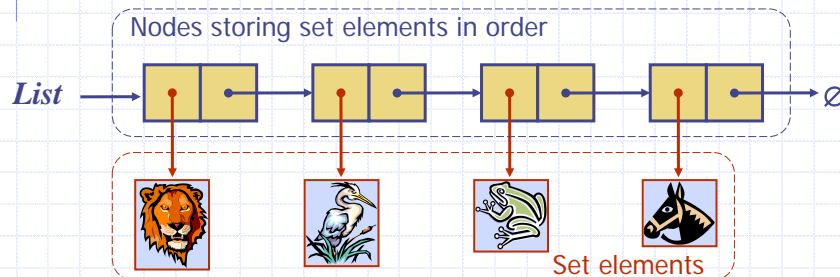
Set Operations



- ◆ We represent a set by the sorted sequence of its elements
- ◆ By specializing the auxiliary methods the generic merge algorithm can be used to perform basic set operations:
 - union
 - intersection
 - subtraction
- ◆ The running time of an operation on sets A and B should be at most $O(n_A + n_B)$
- ◆ Set union:
 - $aIsLess(a, S)$
 $S.insertFront(a)$
 - $bIsLess(b, S)$
 $S.insertBack(b)$
 - $bothAreEqual(a, b, S)$
 $S.insertFront(a)$
- ◆ Set intersection:
 - $aIsLess(a, S)$
{ do nothing }
 - $bIsLess(b, S)$
{ do nothing }
 - $bothAreEqual(a, b, S)$
 $S.insertBack(a)$

Storing a Set in a List

- ◆ We can implement a set with a list
- ◆ Elements are stored sorted according to some canonical ordering
- ◆ The space used is $O(n)$



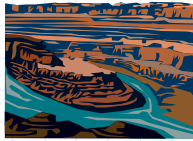
Generic Merging

- ◆ Generalized merge of two sorted lists A and B
- ◆ Template method **genericMerge**
- ◆ Auxiliary methods
 - $aIsLess$
 - $bIsLess$
 - $bothAreEqual$
- ◆ Runs in $O(n_A + n_B)$ time provided the auxiliary methods run in $O(1)$ time

```

Algorithm genericMerge(A, B)
    S ← empty sequence
    while ¬A.empty() ∧ ¬B.empty()
        a ← A.front(); b ← B.front()
        if a < b
             $aIsLess(a, S)$ ; A.eraseFront()
        else if b < a
             $bIsLess(b, S)$ ; B.eraseFront()
        else { b = a }
             $bothAreEqual(a, b, S)$ 
            A.eraseFront(); B.eraseFront()
    while ¬A.empty()
         $aIsLess(a, S)$ ; A.eraseFront()
    while ¬B.empty()
         $bIsLess(b, S)$ ; B.eraseFront()
    return S
    
```

Using Generic Merge for Set Operations



- ◆ Any of the set operations can be implemented using a generic merge
- ◆ For example:
 - For **intersection**: only copy elements that are duplicated in both list
 - For **union**: copy every element from both lists except for the duplicates
- ◆ All methods run in linear time