

# Code

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```
mod = 1_000_000_007

@cache
def dp(n: int, k: int):
    if n == k:
        return 1
    if n <= 0 or k <= 0:
        return 0
    return (dp(n - 1, k - 1) + (n - 1) * dp(n - 1, k)) % mod

class Solution:
    def rearrangeSticks(self, n: int, k: int) -> int:
        return dp(n, k)
```

# What It Does

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For a set  $A = \{1, \dots, n-1\}$ , if new element  $n$  comes in,  $V_k(A' := A \cup \{n\}) = V_{k-1}(A) + (n-1)V_k(A)$

## 1. Place $n$ at rear

If we do so, since  $n$  is larger than any element in  $A$ , we would get  $V_{k-1}(A)$  arrangements with  $k$  visible sticks.

## 2. Place $n$ where it doesn't affect the number of visible elements

We already have  $k$  visibles in  $V_k(A)$  arrangements so we shouldn't affect them. To do so, we have no choice but to place  $n$  just in front of the last visible element,  $n-1$ .

Or we could simply think of a set  $B = \{1, \dots, n-2, n\}$  instead of  $A$  since  $V_k(B) = V_k(A)$ . Also, for any element  $m < n$  and  $X = \{1, 2, \dots, m-1, m+1, \dots, n-1, n\}$ ,  $V_k(X) = V_k(A)$ . So we have  $n-1$  cases in total.